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Charge Distribution and Contact Resistance Model for Coplanar Organic Field-Effect Transistors

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Abstract

We propose a theoretical description of the charge distribution and the contact resistance in coplanar organic field-effect transistors (OFETs). Based on the concept that the current in organic semiconductors is only carried by injected carriers from the electrodes, an analytical formulation for the charge distribution inside the organic layer was derived. We found that the contact resistance in coplanar OFETs arises from a sharp low-carrier-density zone at the source/channel edge because the gate-induced channel carrier density is orders of magnitude higher than the source carrier density. This image is totally different from the contact resistance in staggered OFETs, in which the contact resistance mainly originates from the resistance through the semiconductor bulk. The contact resistance was calculated through charge-distribution functions and the model could explain the effect of the gate voltage and injection barrier on the contact resistance. Experimental data on pentacene OFETs were analyzed using the transmission-line method. We finally noticed that the gate-voltage dependent mobility is a critical factor for proper understanding of the contact resistance in real devices.

Index Terms
Charge distribution, contact resistance, coplanar OFETs, physical modeling.

I. INTRODUCTION

IN SPITE OF impressive advances in organic electronic devices, theoretical understanding of their operation is still incomplete. Organic field-effect transistors (OFETs), which are of great importance for low-cost flexible electronics, need more fundamental insights for further breakthroughs [1]. Among other interesting features of OFETs, contact resistance ($R_c$) effect is decisive because there exists a substantial injection barrier in most realistic metal/organic junctions. In other words, even if one might choose a metal of which the Fermi level is very close to the transport orbital (HOMO or LUMO) of the organic material, process contamination and formation of interface trap states generally result in a Fermi level pinning so that the injection barrier cannot vanish below certain level [2], [3].

It is widely accepted that device geometry plays a crucial role for $R_c$ and comparative experiments on staggered and coplanar structures have been reported [4], [5]. Fig. 1 illustrates four common device geometries of OFETs. Typically, staggered OFETs showed smaller $R_c$ than coplanar OFETs. This tendency was tentatively explained by various concepts including metal penetration into organic films [6] and lateral morphological variation of polycrystalline film [5], [7]. In both geometries, $R_c$ seemed to be also dependent on the applied gate voltage ($V_G$) with its magnitude decreasing with increasing $|V_G|$. Several models based on the current crowding mechanism have been invoked to explain the $V_G$ dependence of $R_c$ in staggered OFETs [8], [9], [10], [11]. However, no such consummate operation model exists for the origin and the $V_G$-dependence of $R_c$ in coplanar OFETs. The coplanar structure is more frequently adopted than the staggered one in fabrication. This is due to the fact that people prefer to avoid metal-deposition damage on a ‘fragile’ organic film in bottom-gate configuration. Therefore, a specific model for coplanar OFETs is highly desired. Concerning the geometrical effect on $R_c$, we recently observed that, apart from the above-mentioned process-related factors, there is a fundamental difference in the ‘charge distribution’ in staggered and coplanar organic transistors and this fact implies an underlying physical background of the dissimilar contact behaviors [12].

Here, we propose a physical device model for coplanar OFETs. Analytical equations for the two-dimensional charge distribution are developed by solving Poisson’s and transport equations and by applying boundary conditions for a finite-thickness semiconductor. The carrier-density in the transition zone at the source/channel interface is modeled to build up a formulation of $R_c$ as an integration of the local resistivity. Numerically calculated $R_c$ clearly shows the influence of $V_G$ and injection barrier height ($E_i$) on the determination of $R_c$. Experimental data on coplanar OFETs are analyzed by testing coplanar pentacene transistors. By applying the transmission-line method (TLM) to the measurement results, it is revealed that the $V_G$-dependence of mobility is another pivotal factor that should be taken into account.

II. EXPERIMENTAL AND MODELING METHODS

Pentacene-based coplanar OFETs were fabricated with the structure equivalent to the the model transistor in Fig. 2. The bottom-gate electrode was prepared by a deposition of Cr on a glass substrate. A chemically and mechanically stable epoxy-based photoresist SU-8 was used as a gate insulator. A diluted SU-8 solution (SU-8 2050 product of MicroChem) was
Fig. 1. Four OFET structures characterized by the relative positions of the gate (G) and the source/drain (S/D) electrodes. By definition, the source/drain electrodes in coplanar OFETs are on the same plane with the conducting channel. In the staggered structure, on the contrary, the semiconducting layer separates the source/drain electrodes from the channel. The model presented in this study is applicable to the two coplanar structures.

Fig. 2. Charge distribution inside the organic semiconductor of a coplanar-type OFET. The analytical curves are obtained by (15), (17), (23), and (27). Note that the device simulator brings very close results.

spin-coated on the substrate and UV-exposed to activate the cross-linking reaction. The processed film was hard-baked at 200 °C for 2 minutes. This method gave a 950 nm-thick polymeric film with the gate capacitance of 2.3 nF/cm². The source/drain electrodes were then formed by depositing Au followed by a photolithographical patterning step. Pentacene (99.9+% purity, used as-received from Sigma-Aldrich) was finally vacuum-evaporated to form a hole-trasporting molecular film. During the thermal evaporation of pentacene, the substrate was heated at 50 °C and the deposition rate was kept at 0.1 nm/s with the final thickness of 50 nm. We have recently estimated the quasistatic dielectric constant of pentacene in [13] and the average value of 3.6 will be used in this study.

Current-voltage (I-V) characteristics were measured using a semiconductor characterization system (Keithley 4200) in the dark under ambient atmosphere. Tapping-mode atomic force microscopy (AFM) images of the pentacene film were taken using Veeco Dimension 5000 AFM system. Model calculations were performed with MATHCAD platform (Parametric Technology Corporation). To support the model, simulation results were taken through two-dimensional physically-based ATLAS simulator (SILVACO). This finite-element computer simulator numerically solves a set of coupled Poisson’s, continuity, and drift-diffusion equations within a user-defined two-dimensional mesh.

III. CHARGE-CARRIER DISTRIBUTION IN AN ORGANIC SEMICONDUCTOR

The aim of this section is to find how the injected holes from the source (pₛ) and the gate-induced holes at the channel (pᶜʰ) are distributed along the thickness of the organic layer (y-axis) in the model transistor depicted in Fig. 2. Throughout this study, a two-dimensional model will be developed based on the following hypotheses: 1) All charge carriers are “injected” into the organic semiconductor; 2) hole-only conduction is considered; 3) the gradual channel approximation holds. We recently confirmed that unintentionally doped organic semiconductors are fully depleted so that the above assumption 1) can be made [13]. By this simplification, an organic semiconductor is rather an insulator that can only ‘transport’ the carriers given by external circumstances (injection or illumination) and we can revisit the classical theory on the metal/insulator junction that
has been intensively dealt with in the early days of solid-state electronics through the 1940s and 1950s. We will first briefly recapitulate traditional models in Section III-A and propose a new approach in Section III-B.

A. Revisiting classical models

Imagine a one-dimensional insulator (or undoped semiconductor) in contact with a charge reservoir (normally a metal electrode) at $y = 0$ that extends toward the positive $y$-direction up to $y = d$ ($d$ is the thickness of the semiconductor). The electrostatic distribution of injected carriers $p(y)$ can be estimated by simultaneously analyzing Poisson’s equation (1) and the transport (drift-diffusion) equation (2)

$$\frac{dF}{dy} = \frac{q p(y)}{\varepsilon_s}, \quad (1)$$

$$J_p = q \mu F - q D \frac{dp}{dy}, \quad (2)$$

where $F(y)$ is the electric field, $q$ the elementary charge, $p(y)$ the hole concentration, $\varepsilon_s$ the permittivity of the semiconductor, $J_p$ the net hole current density, $\mu$ the hole mobility, and $D$ the hole diffusion coefficient. These two equations are then merged by substituting $p$ in (2) using (1) and by taking Einstein relation $D/\mu = kT/q$, where $k$ is the Boltzmann constant and $T$ the absolute temperature. This gives

$$J_p = \varepsilon_s \mu \left( F \frac{dF}{dy} - \frac{kT}{q} \frac{d^2 F}{dy^2} \right),$$

which is the fundamental equation of the given physical system to be solved. At thermal equilibrium, the net current is zero (the drift current and the diffusion current compensate each other) so that

$$F \frac{dF}{dy} - \frac{kT}{q} \frac{d^2 F}{dy^2} = 0. \quad (4)$$

This can be integrated once to

$$\left( \frac{q}{2kT} \right)^2 F^2 - \frac{q}{2kT} \frac{dF}{dy} = -g^2, \quad (5)$$

where $g$ is an integration constant.

Mott and Gurney first derived the solution of (5) for a semi-infinite semiconductor ($d \to \infty$) [14]. In this case, both $F(y)$ and $dF/dy$ go to zero when $y \to \infty$, so that $g = 0$ and (5) reduces to

$$F^2 - \frac{2kT}{q} \frac{dF}{dy} = 0. \quad (6)$$

The solution for the electric field is reached by separating variables,

$$F(y) = \left( -\frac{2kT}{q y_0} \right) \left( \frac{1}{1 + y/y_0} \right) = \frac{F_0}{1 + y/y_0}, \quad (7)$$

where $y_0$ is another integration constant. The hole distribution $p(y)$ is given by the first derivative of $F(y)$;

$$p(y) = \left( \frac{2 \varepsilon_s kT}{q^2 y_0^2} \right) \left( \frac{1}{1 + y/y_0} \right)^2 = \frac{p_0}{(1 + y/y_0)^2}. \quad (8)$$

$F_0$ and $p_0$ are respectively the electric field and the hole concentration at the junction ($y = 0$). Equations (7) and (8) are intended to make more visible the physical meaning of $y_0$, which can be viewed as a characteristic length over which the boundary value ($F_0$ or $p_0$) is distributed from the junction interface. The value of $y_0$ can be determined from the boundary value of either $F_0$ or $p_0$. For the following discussion, a relationship between $y_0$ and $p_0$ is particularly useful. From (8), we have

$$y_0 = \sqrt{\frac{2 \varepsilon_s kT}{q^2 p_0}}, \quad (9)$$

meaning that the higher the initial carrier density $p_0$ is, the smaller $y_0$ becomes. If $y_0$ is small, the carriers are densely concentrated at the junction and do not spread far away from the injecting surface. Even though the Mott-Gurney model provides meaningful insight into the charge distribution, its usage should be limited to very thick organic crystals and this model cannot be safely applied to thin organic films.

Skinner stepped forward and developed more general solutions to (5) [15]. It means that one can challenge the ‘finite’ junction without forcing $g$ to zero. The author actually separated the cases by the sign of the integration constant and obtained separate sets of solutions depending on this sign. An essential boundary condition for the finite semiconductor is $F(d) = 0$ because there cannot be any current flowing into or out of the semiconductor at the surface $y = d$. The injected holes (positive charges) make the only contribution to the space charge in Poisson’s equation. Consequently, the sign of $dF/dy$ is always
positive through the whole semiconductor thickness. In other words, \( F(0) \) is negative and \( F(y) \) approaches zero from \( y = 0 \) to \( y = d \). At \( y = d \), \( F \) becomes zero by the boundary condition and \( dF/dy \) remains positive. Therefore, the right-hand term in (5) is negative and the corresponding solution is the trigonometric function in [15], which can be written in the form;

\[
F(y) = -\frac{q\rho_0 d y_0^2}{\epsilon_s} \cot(g y + \arcsin g y_0),
\]

\[
p(y) = \frac{p_0 d^2 y_0^2}{\sin^2(g y + \arcsin g y_0)}.
\]

Here, \( \rho_0 \) always represents the hole concentration at \( y = 0 \) and (9) remains valid. In order to estimate the constant \( g \), we introduce the boundary condition \( F(d) = 0 \). From (10), this gives

\[
\cot(g d + \arcsin g y_0) = 0,
\]

which can be further simplified by using trigonometric identities, resulting in

\[
g y_0 = \cos g d.
\]

By putting (13) into (11), we can write

\[
p(y) = -\frac{p_0 \cos^2 g d}{\cos^2 g (d - y)},
\]

where \( 0 \leq y \leq d \).

A limitation of Skinner’s approach looks apparent at this point. Although this model gives exact solutions for thin-film cases, (13) does not lead to an analytical expression for \( g \) and, consequently, the final solution requires numerical computation.

B. Approximate solutions

Now let us return to the two-dimensional semiconductor and discuss how the initial carrier densities at the insulator/semiconductor interface \((y = 0)\) are determined in the coplanar OFET architecture (see the inset in Fig. 2). The carrier density at a metal/semiconductor interface is dictated by Boltzmann’s statistics [16] so that \( p_s \) (the source carrier density at \( y = 0 \)) is strongly injection-limited following

\[
p_s = N_v \exp \left(-\frac{E_b}{kT}\right),
\]

where \( N_v \) is the effective density of states at the HOMO edge. The hole barrier height \( E_b \) corresponds the energy between the electrode Fermi level and the semiconductor HOMO level. The channel carriers, on the other hand, are induced by the gate capacitance and can be estimated by

\[
Q_{ch} = C_i |V_G - V_T| = q \int_0^d p_{ch}(y)dy,
\]

where \( Q_{ch} \) is the total channel charge per unit area, \( C_i \) the insulator capacitance per unit area, and \( V_T \) the threshold voltage. The functional form of \( p_{ch}(y) \) will be derived below but it is helpful to know the boundary value already here. The channel hole concentration at \( y = 0 \) is approximate to

\[
p_{ch0} \approx \frac{Q_{ch}^2}{2\epsilon_s kT} = \frac{C_i^2 |V_G - V_T|^2}{2\epsilon_s kT}.
\]

The characteristic distribution lengths for the source and the channel charges are then defined by (9), thus \( y_s = \sqrt{2\epsilon_s kT/q^2p_s} \) and \( y_{ch0} = \sqrt{2\epsilon_s kT/q^2p_{ch0}} \) respectively.

We can infer from (15) and (17) that \( E_b \) and \( V_G \) are the principal parameters for the source and channel distribution of charges. The results presented in Fig. 3 support this statement and give another important implication for the modeling. Fig. 3 shows the results calculated by (15) and (17) with \( N_v = 10^{20} \text{ cm}^{-3} \), \( T = 300 \text{ K} \), \( \epsilon_s = 3.6 \times \epsilon_0 \), \( C_i = 2.3 \text{ nF/cm}^2 \), and \( V_T = 0 \text{ V} \) (\( \epsilon_0 \) is the permittivity of vacuum). Typical organic materials exhibit a transport band width of around 500 meV, which is much larger than the thermal energy \( kT \). In this case, \( N_v \) should be lower than the total molecular density and \( 10^{20} \text{ cm}^{-3} \) is a realistic value for \( N_v \). At variance with the charge distribution in staggered OFETs in which the gate-induced charges are evenly distributed over the whole semiconductor/insulator interface [12], here \( p_{ch0} \) is much lower than \( p_{ch0} \) due to the high injection barrier. Another key feature of Fig. 3 is that \( y_{ch0} \) normally exceeds the thickness of an organic thin-film, whereas \( y_{ch0} \) is far smaller than the film thickness. This finding enables an independent modeling of \( p_s(y) \) and \( p_{ch}(y) \) by means of an approximation method.

The main idea is to develop an analytical form of (14) by approximating the cosine function in (13). A linear (or a first-order) approximation of any given function \( f(z) \) is defined at the vicinity of \( z = a \) by

\[
f(z) \approx f(a) + f'(a)(z - a).
\]
If \( f(z) = \cos z \), we get
\[
\cos z \approx \cos a + (-\sin a)(z - a).
\] (19)

First, for the source carriers \( p_s(y) \), we rewrite (13) as
\[
g_s y_{s0} = \cos g_s d,
\] (20)
where the subscript ‘s’ refers to the ‘source’. Because \( y_{s0} \gg d \), we can approximate \( \cos g_s d \) where \( g_s d \) is close to zero. Under this condition, we can say
\[
g_s y_{s0} = \cos g_s d \approx 1,
\] (21)
and therefore
\[
g_s \approx \frac{1}{y_{s0}}.
\] (22)

Then if we use (22) to replace \( g \), (14) finally changes into
\[
p_s(y) = p_{s0} \frac{\cos^2 \left( \frac{d}{y_{s0}} \right)}{\cos^2 \left( \frac{d - y}{y_{s0}} \right)}.
\] (23)

Next, another approximation is needed for the channel carriers \( p_{ch}(y) \). Starting again from (13),
\[
g_{ch} y_{ch0} = \cos g_{ch} d,
\] (24)
where the subscript ‘ch’ refers to the ‘channel’. This time, \( y_{ch0} \ll d \) so that \( \cos g_{ch} d \) should be developed near \( g_{ch} d = \pi/2 \). Referring to (19), we get
\[
g_{ch} y_{ch0} = \cos g_{ch} d \approx \frac{\pi}{2} - g_{ch} d,
\] (25)
and
\[
g_{ch} \approx \frac{\pi}{2(d + y_{ch0})}.
\] (26)

The channel carrier distribution function \( p_{ch}(y) \) is now given from (14) and (26), after some manipulation steps, by
\[
p_{ch}(y) = p_{ch0} \frac{\sin^2 \left( \frac{\pi y_{ch0}}{2} \right)}{\sin^2 \left( \frac{\pi (y_{ch0} + y)}{2d} \right)}.
\] (27)

Now one can reexamine the integration in (16) and see that (17) is correct under the condition that \( y_{ch0} \ll d \).

It is worth emphasizing here that our approximate model [(23) and (27) with (15) and (17)] provides analytical expressions that explicitly contain the thickness parameter \( d \). It means that this strategical development overcomes the limitation of the two classical models summarized in Section III-A and assures its general applicability to the thin film-based OFETs. Fig. 2 shows the reliability of the approximate solutions. The parameters used here in both the analysis and the simulation are those listed above for Fig. 3 with \( d = 50 \) nm, \( E_b = 0.3 \) eV, and \( V_G = -20 \) V. It is shown that the analytical model predicts the numerical simulation results with satisfying precision.
IV. Charge-based contact resistance model

Now that we have a two-dimensional picture of the charge distribution inside the organic film in coplanar OFETs, we develop a charge-based contact resistance model in this section. Section IV-A will deal with a mathematical formulation of $R_c$ in the transition zone and the effect of the critical parameters will be discussed in Section IV-B.

A. Resistance of the transition zone

We realize that there is an abrupt transition of the hole concentration at $x = 0$ due to the huge difference between $p_s(y)$ and $p_{ch}(y)$. It is this carrier-density transition zone that accounts for the origin of $R_c$ because the hole concentration in this zone is much lower than that in the conducting channel, due to the effect of $p_s$ penetrating into the channel region. Now let us contemplate what happens at this source/channel interface where two independent distribution functions overlap (Fig. 4). There exist concentration tails along the $x$-direction characterized by the Debye length of the channel carriers ($x_{ch}$) and that of the source carriers ($x_s$). They are defined by $x_{ch} = \sqrt{\frac{\varepsilon_s kT}{q^2 p_{ch}}}$ and $x_s = \sqrt{\frac{\varepsilon_s kT}{q^2 p_s}}$ [16]. Because $p_{ch} \gg p_s$, $x_{ch} \ll x_s$ and we can neglect the contribution of $x_{ch}$ so that the transition from $p_s$ to $p_{ch}$ can be simplified to a single exponential function

$$p(x) = p_s \exp\left(\frac{x}{x_s}\right), \quad (28)$$

Then the thickness $t$ of the transition zone in Fig. 4 is estimated by

$$p(t) = p_s \exp\left(\frac{t}{x_s}\right) = p_{ch}, \quad (29)$$

$$t = x_s \ln\left(\frac{p_{ch}}{p_s}\right). \quad (30)$$

Here, it is worth mentioning that $t$ also varies along the semiconductor thickness as $p_{ch}$ and $p_s$ change together along the $y$-direction. Taking the parameters used in Section III-B, the calculated $t$ is 0.51 µm at $y = 0$. It means that only a narrow region of the entire channel near the source electrode is affected by low $p_s$.

The contact resistance $R_c$ is calculated from an estimation of the average hole concentration in the transition zone (or $R_c$ zone), done by integrating the local conductivity over the entire thickness. Keeping this approach in mind, the mean hole concentration $p_m$ throughout the $R_c$ zone can be defined by

$$p_m = \frac{1}{t} \int_0^t p(x) dx = \frac{p_s}{t} \int_0^t \exp\left(\frac{x}{x_s}\right) dx, \quad (31)$$

where (28) is used. By inserting (29) and (30) and using $p_{ch} \gg p_s$, we get

$$p_m = \frac{p_{ch} - p_s}{\ln(p_{ch}/p_s)} \approx \frac{p_{ch}}{\ln(p_{ch}/p_s)}, \quad (32)$$

which shows that the balance between $p_s$ and $p_{ch}$ determines the average concentration and $p_m$ is also a function of $y$. Now we can calculate the elemental conductance $dG_c$ of the volume element delimited by $W$ (channel width), $t(y)$, and $dy$.

$$dG_c = q\mu_W \frac{p_m(y)}{t(y)} dy, \quad (33)$$
\[ R_c = \frac{1}{G_c} = \sqrt{\frac{\varepsilon_s kT}{q^2 \mu W}} \left[ \int_0^d \frac{p_{ch}(y) \sqrt{p_s(y)}}{\ln(p_{ch}(y)/p_s(y))} \, dy \right]^{-1}. \] (34)

Note that, from (34), it is possible to predict the exact value of \( R_c \) when the distribution functions for \( p_s(y) \) and \( p_{ch}(y) \) are known.

B. Effect of the parameters

Numerically calculated \( R_c \) values are plotted in Fig. 5 with varying \( V_G \) and \( E_b \). The charge-distribution functions \([ p_s(y) \) and \( p_{ch}(y) \)] developed in Section III-B were inserted to (34). All fixed parameters are summarized in the caption to Fig. 5. We can state, from this result, that the theoretical charge-based model well predicts the decrease of \( R_c \) with increasing \( |V_G| \), which is often experimentally observed, though not sufficiently understood in the case of coplanar OFETs [17], [18], [19], [20]. Furthermore, it can be inferred that the degree of dependency between \( V_G \) and \( R_c \) is accentuated with higher injection barriers. Finally, it should be noted that the hole mobility \( \mu \) is considered constant here, which restricts the analysis to defect-free, highly pure crystalline semiconductors [21]. When substantial trap states exist, \( \mu \) should be regarded as the ‘effective’ mobility determined by the ratio of free to total carrier density. This results in the dependence of the measured mobility on the gate voltage as will be discussed in the next section.

V. APPLICATION TO EXPERIMENTAL RESULTS

This section is dedicated to the analysis of experimental results on fabricated OFETs with the \( R_c \) model. In Section V-A, the basic electrical properties of pentacene-based OFETs will be presented. Then, in Section V-B, we will concisely summarize how the transmission-line method works for experimentally extracting \( R_c \). Finally, the \( V_G \)-dependent mobility and its influence on \( R_c \) will be discussed in Section V-C.
A. Output and transfer curves

The electrical performance of a representative transistor is shown in Fig. 6. The channel width $W$ and length $L$ of this transistor are 500 $\mu$m and 20 $\mu$m respectively. The slight upward bending of the output curves [Fig. 6(a)] at low drain voltage ($V_D$) is direct evidence for a non-linear parasitic contact effect [18]. Hence, it can be predicted that there is non-negligible contribution of $R_c$ to the current in the fabricated device. A linear-regime transfer curve is shown in Fig. 6(b). One can see that the off-state current is extremely low and close to the detection limit of the measurement system ($10^{-12}$ A), assuring an excellent gate-insulation by the SU-8 film. The AFM image in Fig. 6(b) shows relatively small domain size of the order of 100 nm. These small and uniform grains could be attributed to the three-dimensional growth of pentacene which contrasts with the two-dimensional layer-by-layer growth that results in large, dendritic grains [22].

B. Transmission-line method

The transmission-line method (TLM) is a widely-used technique for the extraction of $R_c$ from $I$-$V$ data [23], [24], [25]. It is assumed that the source-to-drain current path is equivalent to a series combination of contact resistance $R_c$ and channel resistance $R_{ch}$ (inset in Fig. 7). The TLM is also strongly based on the assumption that $R_c$ is not a function of $L$ but $R_{ch}$ is proportional to $L$ [26]. At low $V_D$ (linear regime), the relationship between $I_D$ and $V_D$ of this circuit can be expressed as

$$I_D = \frac{V_D}{R_{on}} = \frac{V_D}{R_c + R_{ch}} = \frac{V_D}{R_c + \left[ \frac{W}{L} \mu C_i |V_G - V_T| \right]^{-1}},$$

(35)

where the linear-regime channel conductance is used to estimate $R_{ch}$. $R_{on}$ is the on-state resistance that can be directly obtained from measured $V_D$ and $I_D$ by

$$R_{on} = \frac{V_D}{I_D} = \frac{L}{W \mu C_i |V_G - V_T|}.$$

(36)

Width-normalized resistance is more practical for the purpose of comparing device sets with different $W$ so it is useful to multiply (36) by $W$ and get

$$R_{on} \times W = R_c \times W + \frac{L}{\mu C_i |V_G - V_T|}.$$  

(37)

To apply the TLM, we first draw $R_{on} W$ versus $L$ and extrapolate the linear regression line to zero $L$ to read the $R_c W$ value. Fig. 7 shows the experimental data on pentacene OFETs. The deviation of the data points from the regression lines is minimal and it makes sure that the fabricated OFETs well satisfy the basic assumptions of the TLM. It is clear that $R_c$ decreases with increasing $|V_G - V_T|$ as the intercept to the vertical axis moves downward. $V_T$ for those three transistors were evaluated from the saturation current and no significant variation was observed so that we can use an average $V_T$ of -4 V. Although not often realized, it is important to note here that the TLM can also be used to estimate $\mu$ as a function of $|V_G - V_T|$ because the ‘slope’ of the regression line usually varies with $V_G$ (see Fig. 7) and this slope contains the parameter $\mu$ by (37).
Fig. 7. $R_{on}W$ versus $L$ plot for the transmission-line method (TLM). The inset is the equivalent circuit of the on-state conduction path that consists of a series connection of the contact and channel resistances. Note that $R_c$ and $R_{ch}$ are drawn as variable resistors because both of them are supposed to be $V_G$-controlled.

Fig. 8. Hole mobility as a function of $|V_G - V_T|$ extracted by the TLM. The solid line is a fit to the trap-filling model at low $|V_G|$. The decrease in the mobility at higher $|V_G|$ can be attributed to the field-induced mobility degradation.

C. Effect of the gate-voltage dependent mobility

The extracted hole mobility $\mu$ as a function of $|V_G - V_T|$ is shown in Fig. 8, which indicates that the variation of $\mu$ is significant and does not follow a simple monotonous behavior. We infer that the two distinct regimes are dominated by two different mechanisms. First, the rise in $\mu$ at low $|V_G|$ can be adequately described by the gradual filling of trap states as the Fermi level at the semiconductor/insulator interface approaches the transport orbital (HOMO in the case of p-type materials). This is reasonable because a polycrystalline pentacene film contains a large number of trapping sites, most of which located at the grain boundaries [27], [28]. We refer to the model of Horowitz et al. [29], [26] and fit the mobility in this regime
Fig. 9. TLM-extracted $R_cW$ as a function of $|V_G - V_T|$ in comparison to the charge-based model developed in Section IV. Note that, if a constant mobility is assumed (here 0.2 cm$^2$/V·s), the $V_G$-dependence of $R_c$ is underestimated. When we take the $V_G$-dependent mobility into account, the experimental results could be well fitted by the model. This method also enables an estimation of the injection barrier $E_b$.

\begin{equation}
|V_G - V_T| < 30 \text{ V} \end{equation}

This model is based on the MTR (multiple trapping and release) process with an exponential density of states (DOS) near the band edge. The parameters $\kappa$ and $\alpha$ are then related to the trap DOS. The exponent $\alpha$ is directly linked to the trap characteristic temperature $T_c$ by $\alpha + 1 = (T_c/T)$. The extracted $\alpha$ is 1.35 in Fig. 8 and the corresponding $T_c$ is 705 K. If we convert this value into energy scale, the trap distribution width $E_t = kT_c$ is 61 meV, which is in good agreement with a recent comprehensive review on the trap DOS in pentacene field-effect transistors [30]. Next, the slight decrease in $\mu$ at higher $|V_G - V_T|$ can be interpreted by the field-induced mobility degradation [22]. It is likely that the mobility near the insulator surface is lower than that at the bulk region due to various surface scattering agents. When $|V_G|$ becomes high enough, field-induced holes are more concentrated at this low-mobility near-insulator region so that the effective mobility of the conduction path could be reduced.

Fig. 9 shows how seriously the $V_G$-dependent mobility affects the charge-based $R_c$ model. Here, the TLM-extracted $R_c$ values are plotted as a function of $|V_G - V_T|$. As expected, $R_c$ decreases rapidly with increasing $|V_G - V_T|$. We simply replaced $\mu$ in (34) by (38) and calculated $R_c$ to compare with the experimental curve. Note that the entire curve in Fig. 8 cannot be modeled by a simple analytical expression, so we only took the trap-dominated regime ($|V_G - V_T| < 30$ V) for the analysis in Fig. 9. As emphasized in Section IV-B, $V_G$ and $E_b$ are the foremost parameters that govern $R_c$. Therefore, by optimizing the TLM-extracted curve with the model, we could effectively estimate the injection barrier $E_b$ at the Au/pentacene interface in the fabricated OFETs. One can see that the model-calculated curve is in very good agreement with the experimental curve with $E_b$ of 0.38 eV. When we calculated $R_c$ with a constant mobility of 0.2 cm$^2$/V·s, the model could not accurately predict the experimental results.

In the literature, there has been a question about how sometimes $R_c$ is less sensitive to $V_G$ or even assumed to be constant [31], [12] while more often $R_c$ is strongly dependent on $V_G$. For coplanar OFETs, the whole picture of this study can suggest two answers: First, the injection barrier $E_b$ plays an important role on the dependence of $R_c$ on $V_G$ (Fig. 5) thus the material combination of the metal and the semiconductor is basically crucial [32]. Second, $V_G$-dependent mobility can either intensify or diminish the slope of an $R_c$ versus $V_G$ curve, because $\mu$ can either increase or decrease (or even remain stable) with $V_G$, depending on various geometrical and/or electrical mechanisms [22], [29], [33], [34].

VI. CONCLUSION

In this study, a physical model for coplanar OFETs has been presented. Starting from the coupled Poisson’s and transport equations, we could formulate an approximate analytical model for the charge distribution inside an organic semiconductor. The distribution functions were inspired by the classical theory of metal/insulator contacts because unintentionally doped organic
semiconductors are characterized by very low thermal carrier density. The origin of the contact resistance was attributed to a low-carrier-density zone at the source/channel edge. An equation for the contact resistance was suggested and the model could explain the gate-voltage dependence of the contact resistance. Pentacene-based OFETs were fabricated and analyzed by the transmission-line method. It was found that, in most cases, the mobility is strongly dependent on the gate-voltage and this effect can further complicate the dependence of the contact resistance on the gate-voltage. We believe that this model can be widely applied for interpreting and predicting the behavior of coplanar OFETs and will deepen the fundamental understanding of the device physics of organic devices.

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**REFERENCES**


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