Some remarks on wheeled autonomous vehicles and the evolution of their control design

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Abstract: Recent investigations on the longitudinal and lateral control of wheeled autonomous vehicles are reported. Flatness-based techniques are first introduced via a simplified model. It depends on some physical parameters, like cornering stiffness coefficients of the tires, friction coefficient of the road, . . . , which are notoriously difficult to identify. Then a model-free control strategy, which exploits the flat outputs, is proposed. Those outputs also depend on physical parameters which are poorly known, i.e., the vehicle mass and inertia and the position of the center of gravity. A totally model-free control law is therefore adopted. It employs natural output variables, namely the longitudinal velocity and the lateral deviation of the vehicle. This last method, which is easily understandable and implementable, ensures a robust trajectory tracking problem in both longitudinal and lateral dynamics. Several convincing computer simulations are displayed.

1. INTRODUCTION

The lateral and longitudinal control of wheeled autonomous vehicles is an important topic which has already attracted many promising studies (see, e.g, Ackermann et al. [1995], d'Andréa-Novel et al. [2001], Antonov et al. [2008], Attia et al. [2014], Choi et al. [2009], Cerone et al. [2009], Chou et al. [2005], Fuchshumer et al. [2005], Marino et al. [2005], Martinez et al. [2007], Menhour et al. [2011], Nouvelière [2002], Poussot-Vassal et al. [2011], Rajamani et al. [2000], Villagra et al. [2009, 2011, 2012], Zheng et al. [2006], . . .), where various advanced theoretical tools are utilized. This short communication does not permit unfortunately to summarize them. Let us nevertheless notice that most of them are model-based. The aim of this presentation is to explain and justify the evolution of our viewpoint which started with a flatness-based setting (Menhour et al. [2011]), i.e., a model-based approach. It is now adopting a fully model-free standpoint (see Menhour

et al. [2013] and Menhour et al. [2015]). As a matter of fact severe difficulties are encountered to

- write a mathematical model which takes into account all the numerous complex phenomena,
- calibrate the existing model in various changing situations like cornering stiffness coefficients of the tires, and friction coefficient of the road.

Our paper is organized as follows. Section 2 presents a nonlinear longitudinal and lateral flatness-based control. In Section 3 the two different model-free control strategies are developed. Simulation results with noisy data and suitable reference trajectories acquired on a track race, are displayed in Section 4. Let us emphasize that the second model-free control is quite robust. Concluding remarks may be found in Section 5.

2. LONGITUDINAL AND LATERAL FLATNESS-BASED CONTROL

2.1 3DoF NonLinear Two Wheels Vehicle Model

The 3DoF-NLTWVM in Figure 1, which is used to design the combined control law, provides an interesting approximation of the longitudinal and lateral dynamics of the vehicle in normal driving situations. See Table 1 for the notations.

Table 1.

| Symbol	Variable name
V_x	longitudinal speed $[km.h]$
V_y	lateral speed $[km.h]$
a_x	longitudinal acceleration $[m/s^2]$
a_y	lateral acceleration $[m/s^2]$
$\dot\psi$	yaw rate $[rad/s]$
ψ	yaw angle $[rad]$
β	sideslip angle $[rad]$
$\alpha_{f,r}$	front and rear tire slip angles $[rad]$
ω_i	wheel angular speed of the wheel i $[rad/s]$
T_ω	wheel torque $[Nm]$
δ	wheel steer angle $[deg]$
C_f, C_r	front and rear cornering stiffnesses $[N.rad\ ^1]$
F_{xi}	longitudinal forces in vehicle coordinate $[N]$
F_{yi}	lateral forces in vehicle coordinate $[N]$
F_{xf}	front longitudinal forces in tire coordinate $[N]$
F_{yf}	front lateral forces in tire coordinate $[N]$
R	tire radius $[m]$
g	acceleration due to gravity $[m/s^2]$
L_f	distances from the CoG to the front axles $[m]$
L_r	distances from the CoG to the rear axles $[m]$
I_z	yaw moment of inertia $[kgm^2]$
I_r	wheel moment of inertia $[kgm^2]$
m	vehicle mass $[kgm^2]$
M_z	yaw moment $[Nm]$
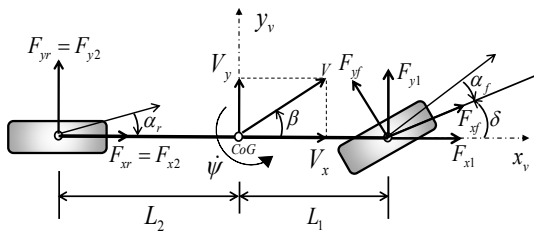
Fig. 1. Nonlinear two wheels vehicle control model

The corresponding dynamical equations read:

$$\begin{cases} ma_x = m(\dot V_x \quad \dot\psi V_y) = (F_{x1} + F_{x2}) \\ ma_y = m(\dot V_y + \dot\psi V_x) = (F_{y1} + F_{y2}) \\ I_z\ddot\psi = M_{z1} + M_{z2} \end{cases}$$

If a linear tire model with small slip angles is assumed (see Menhour et al. [2011] for more details), C_r (resp. C_f) denoting the cornering stiffness coefficient of the rear (resp. front) wheel, and ω_r (resp. ω_f) being the angular velocity of the rear (resp. front) wheel, the previous system can be rewritten:

$$\dot x = f(x,t) + g(x,t)u \tag{1}$$

with

$$f(x,t) = \begin{bmatrix} \dot\psi V_y - \frac{I_r}{mR}(\dot\omega_r + \dot\omega_f) \\ -\dot\psi V_x + \frac{1}{m}\left(-C_f\left(\frac{V_y+L_f\dot\psi}{V_x}\right) - C_r\left(\frac{V_y-L_r\dot\psi}{V_x}\right)\right) \\ \frac{1}{I_z}\left(-L_f C_f\left(\frac{V_y+L_f\dot\psi}{V_x}\right) + L_r C_r\left(\frac{V_y-L_r\dot\psi}{V_x}\right)\right) \end{bmatrix}$$

$$g(x,t) = \begin{bmatrix} \dfrac{1}{mR} & \dfrac{C_f}{m}\left(\dfrac{V_y+L_f\dot\psi}{V_x}\right) \\ 0 & (C_f R - I_r\dot\omega_f)/mR \\ 0 & (L_f C_f R - L_f I_r\dot\omega_f)/I_z R \end{bmatrix}, \quad x = \begin{bmatrix} V_x \\ V_y \\ \dot\psi \end{bmatrix}$$

$$u = [\, u_1 = T_\omega,\ u_2 = \delta\,]^T.$$

2.2 Flatness property

The system $\dot x = f(x,u)$, where $x = (x,\cdots,x_n) \in \mathbb{R}^n$ and $u = (u,\cdots,u_m) \in \mathbb{R}^m$, is said to be *differentially flat* (see Fliess et al. [1995, 1999], and Åström et al. [2008], Lévine [2009], Sira-Ramírez et al. [2004]) if, and only if,

- there exists a vector-valued function h such that
$$y = h(x,u,\dot u,\cdots,u^{(r)}) \tag{2}$$
  where $y = (y,\cdots,y_m) \in \mathbb{R}^m$, $r \in \mathbb{N}$;
- the components of $x = (x,\cdots,x_n)$ and $u = (u,\cdots,u_m)$ may be expressed as
$$x = A(y,\dot y,\cdots,y^{(r_x)}), \quad r_x \in \mathbb{N} \tag{3}$$
$$u = B(y,\dot y,\cdots,y^{(r_u)}), \quad r_u \in \mathbb{N} \tag{4}$$

Remember that y in Equation (2) is called a *flat output*.

2.3 Flatness-based longitudinal and lateral control

Problem 1. Introduce the outputs:

$$\begin{cases} y_1 = V_x \\ y_2 = L_f m V_y - I_z\dot\psi \end{cases} \tag{5}$$

We want to show that the longitudinal speed y_1 and the angular momentum y_2 of a point on the axis between the centers of the front and rear axles are flat outputs.

Proof 1. Some algebraic manipulations (see Menhour et al. [2011] for more details) yield:

$$x = \begin{bmatrix} V_x & V_y & \dot\psi \end{bmatrix}^T = A(y_1,y_2,\dot y_2) =$$
$$\begin{bmatrix} y_1 \\ \frac{y_2}{L_f m} \quad \frac{I_z}{L_f m}\left(\frac{L_f m y_1 \dot y_2 + C_r(L_f+L_r)y_2}{C_r(L_f+L_r)(I_z \quad L_r L_f m)+(L_f m y_1)^2}\right) \\ \left(\frac{L_f m y_1 \dot y_2 + C_r(L_f+L_r)y_2}{C_r(L_f+L_r)(I_z \quad L_r L_f m)+(L_f m y_1)^2}\right) \end{bmatrix} \tag{6}$$

and

$$\begin{bmatrix} \dot y_1 \\ \ddot y_2 \end{bmatrix} = \Delta(y_1,y_2,\dot y_2)\begin{pmatrix} u_1 \\ u_2 \end{pmatrix} + \Phi(y_1,y_2,\dot y_2) \tag{7}$$

The flatness property holds if the matrix $\Delta(y_1,y_2,\dot y_2)$ is invertible:

$$\det(\Delta(y_1,y_2,\dot y_2)) = \Delta_{11}\Delta_{22} - \Delta_{21}\Delta_{12} =$$
$$\frac{(I_\omega\dot\omega_f - C_f R)\left(L_f^2 y_1^2 m^2 - Cr(L_f+L_r)L_r L_f m + C_r I_z L\right)}{I_z R^2 y_1 m^2} \neq 0 \tag{8}$$

This determinant, which only depends on the longitudinal speed $y_1 = V_x$, is indeed nonzero:

- Acceleration of the wheel rotation is less than $RC_f/I_\omega \approx 10^4$. Thus

$$I_\omega \dot{\omega}_f - C_f R \neq 0 \qquad (9)$$

- From $I_z > L_f m$, we deduce that

$$C_r(L_r + L_f)(I_z - L_f m) + L_f^2 m^2 y_1^2 \neq 0 \qquad (10)$$

Thus

$$u = \begin{bmatrix} T_\omega \\ \delta \end{bmatrix} = B(y_1, \dot{y}_1, y_2, \dot{y}_2, \ddot{y}_2) =$$
$$\Delta^{-1}(y_1, y_2, \dot{y}_2) \left(\begin{bmatrix} \dot{y}_1 \\ \ddot{y}_2 \end{bmatrix} - \Phi(y_1, y_2, \dot{y}_2) \right) \qquad (11)$$

with $r_x = 1$ and $r_u = 2$.

A tracking feedback control   In order to track the desired output trajectories y_1^{ref} and y_2^{ref}, set

$$\begin{bmatrix} \dot{y}_1 \\ \ddot{y}_2 \end{bmatrix} = \begin{bmatrix} \dot{y}_1^{ref} + K_1^1 e_{y_1} + K_1^2 \int e_{y_1} dt \\ \ddot{y}_2^{ref} + K_2^1 \dot{e}_{y_2} + K_2^2 e_{y_2} + K_2^3 \int e_{y_2} dt \end{bmatrix} \qquad (12)$$

where, $e_{y_1} = y_1^{ref} - y_1 = V_x^{ref} - V_x$ and $e_{y_2} = y_2^{ref} - y_2$. Choosing the gains K_1^1, K_1^2, K_2^1, K_2^2 and K_2^3 is straightforward.

2.4 Algebraic nonlinear estimation

The control law contains derivatives of measured signals, which are of course noisy. This estimation is performed using the recent advances in Fliess *et al.* [2008], Mboup *et al.* [2005], Sira-Ramírez *et al.* [2014]. It yields the following formulae (García Collado *et al.* [2009]), and, therefore, simple linear digital filters:

- Denoising:

$$\hat{y}(t) = \frac{2!}{T^2} \int_{t-T}^{t} (3(t-\tau) - T) y(\tau) d\tau \qquad (13)$$

- Numerical differentiation of a noisy signal:

$$\hat{\dot{y}}(t) = -\frac{3!}{T^3} \int_{t-T}^{t} (2T(t-\tau) - T) y(\tau) d\tau \qquad (14)$$

The sliding time window $[t - T, t]$ may be quite short.

3. MODEL-FREE DESIGN FOR VEHICLE CONTROL

3.1 Model-free design: motivation

Realistic vehicle models are usually unsuitable for an implementable control design. The above nonlinear flat controller provides good results with known nominal values of the cornering stiffnesses C_f and C_r. Uncertainties on C_f and C_r yield unsatisfactory closed-loop performances: see Figure 2. It is well known that C_f and C_r are very sensitive to high dynamic loads. Figure 3 displays different dynamics of the front and rear cornering stiffness coefficients C_f and C_r during an experimental braking maneuver.
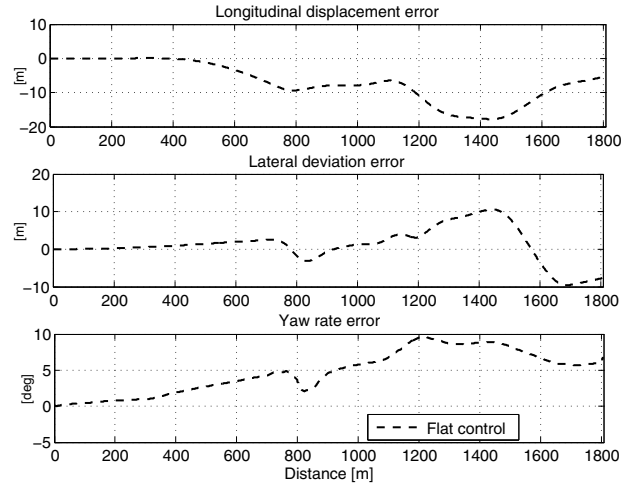

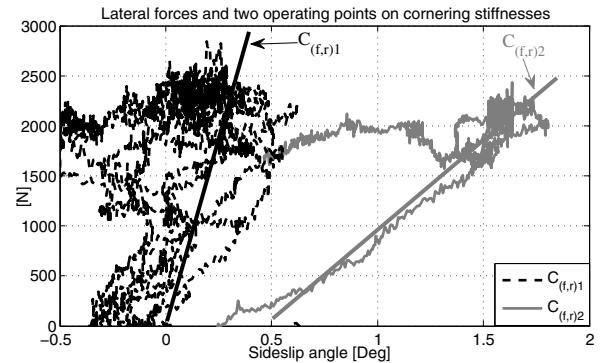Fig. 2. Simulation test with $0.3C_f$ and $0.3Cr$: trajectory tracking with nonlinear flatness-based vehicle control

Fig. 3. Experimental lateral force characteristic and variations of cornering stiffness coefficients (C_f and C_r)

3.2 A short review on model-free control [1]

Model-free control (Fliess *et al.* [2013]) was already successfully used in many concrete case-studies (see, *e.g.*, Fliess *et al.* [2013], and Bara *et al.* [2016], Lafont *et al.* [2015]; the references therein provide numerous other examples). Let us insist here on the already existing applications to vehicles: Choi *et al.* [2009], Formentin *et al.* [2013], Menhour *et al.* [2015], Villagra *et al.* [2009, 2012].

The ultra-local model   Replace the unknown SISO system by the *ultra-local model*:

$$y^{(\nu)} = F + \alpha u \qquad (15)$$

where

- $\nu \geq 1$ is the derivation order,
- $\alpha \in \mathbb{R}$ is chosen such that αu and $y^{(\nu)}$ are of the same order of magnitude,
- ν and α are chosen by the practitioner.

Remark 1. In all the existing concrete examples $\nu = 1$ or 2. Magnetic bearings (de Miras *et al.* [2013]) with their low friction provide the only instance where $\nu = 2$ (see Fliess *et al.* [2013] for an explanation).

Some comments on F are in order:

[1] See Fliess *et al.* [2013] for more details and further explanations. See Join *et al.* [2013] for a cheap hardware implementation. Both references show the online character of this setting, This fact has been confirmed by many concrete case-studies.

- F is estimated via the measurements of the input u and the output y,
- F does not distinguish between model mismatches and perturbations.

Intelligent controllers   Set $\nu = 2$ in Equation (15):

$$\ddot{y} = F + \alpha u \qquad (16)$$

The corresponding *iPID, i.e, intelligent Proportional-Integral -Derivative controller*, reads

$$u = -\frac{\left(F - \ddot{y}^d + K_P e + K_I \int edt + K_D \dot{e}\right)}{\alpha} \qquad (17)$$

where

- y^d is the reference trajectory,
- $e = y - y^d$ is the tracking error and y^d is a desired signal,
- K_P, K_I, $K_D \in \mathbb{R}$ are the usual gains.

Combining Equations (16) and (17) yields

$$\ddot{e} + K_P e + K_I \int edt + K_D \dot{e} = 0$$

where F does not appear anymore. Gain tuning becomes therefore quite straightforward. This is a major benefit when compared to "classic" PIDs (see, *e.g.*, Åström *et al.* [2006, 2008]). If $K_I = 0$ we obtain the *intelligent Proportional-Derivative controller*, or *iPD*,

$$u = -\frac{\left(F - \ddot{y}^d + K_P edt + K_D \dot{e}\right)}{\alpha} \qquad (18)$$

Set $\nu = 1$ in Equation (15):

$$\dot{y} = F + \alpha u \qquad (19)$$

The corresponding *intelligent Proportional-Integral controller*, or *iPI*, reads:

$$u = -\frac{\left(F - \dot{y}^d + K_P e + K_I \int edt\right)}{\alpha} \qquad (20)$$

If $K_I = 0$ in Equation (20), we obtain the *intelligent proportional controller*, or *iP*, which, until now, turns out to be the most useful intelligent controller:

$$u = -\frac{F - \dot{y}^* + K_P e}{\alpha} \qquad (21)$$

Algebraic estimation of F F in Equation (15) is assumed to be "well" approximated by a piecewise constant function F_{est}. According to the algebraic parameter identification due to Fliess *et al.* [2003, 2008] (see also Sira-Ramírez *et al.* [2014]), rewrite, if $\nu = 1$, Equation (19) in the operational domain (see, *e.g.*, Yosida [1984])

$$sY = \frac{\Phi}{s} + \alpha U + y(0)$$

where Φ is a constant such that $\frac{\Phi}{s}$ is the operational transform of F which is supposed to be constant on the sliding window. We get rid of the initial condition $y(0)$ by multiplying both sides on the left by $\frac{d}{ds}$:

$$Y + s\frac{dY}{ds} = -\frac{\Phi}{s^2} + \alpha \frac{dU}{ds}$$

Noise attenuation is achieved by multiplying both sides on the left by s^{-2}. It yields in the time domain the real time estimation

$$F_{\text{est}}(t) = -\frac{6}{\tau^3} \int_{t-\tau}^{t} \left[(\tau - 2\sigma)y(\sigma) + \alpha\sigma(\tau - \sigma)u(\sigma)\right] d\sigma \qquad (22)$$

where $\tau > 0$ may be quite small. This integral may of course be replaced in practice by a classic digital filter. The extension to $\nu = 2$ is given by the following estimator:

$$F_{\text{est}}(t) = \begin{bmatrix} -\dfrac{60}{\tau^5} \displaystyle\int_{t-\tau}^{t} (\tau^2 + 6\sigma^2 - 6\tau\sigma)y_2(\sigma)d\sigma \\ -\dfrac{30\alpha}{\tau^5} \displaystyle\int_{t-\tau}^{t} (\tau - \sigma)^2\sigma^2 u_2(\sigma)d\sigma \end{bmatrix} \qquad (23)$$

3.3 Model-free vehicle control and flat outputs

The only parameters supposed to be known are those used to compute y_2 in Equation (5): the vehicle mass, the yaw moment of inertia and the position of the center of gravity. The control variables are:

- the braking and traction wheel torques to control longitudinal motion,
- the steering angle to control lateral and yaw motions.

The control variables $u_1 = T_\omega$ and $u_2 = \delta$ are respectively the braking and traction wheel torques, and the steering angle. From (11), the following two ultra-local models of longitudinal and lateral motions are derived:

$$\text{longitudinal ultra-local model: } \dot{y}_1 = F_1 + \alpha_1 u_1$$

$$\text{lateral ultra-local model: } \dot{y}_2 = F_2 + \alpha_2 u_2$$

u_1 and u_2 represent respectively the wheel torque control of longitudinal motion y_1 and the steering angle control of lateral and yaw motions y_2. The tracking is achieved by two decoupled multivariable iPIs. Set, according to Equation (20), for the longitudinal iPI controller $u_1 = \frac{1}{\alpha_1}\left(F_1 + \dot{y}_1^d - K_P^{y_1}e_{y_1} - K_I^{y_1}\int e_{y_1}dt\right)$, and for the lateral iPI controller $u_2 = \frac{1}{\alpha_2}\left(F_2 + \dot{y}_2^d - K_P^{y_2}e_{y_2} - K_I^{y_2}\int e_{y_2}dt\right)$, where $e_{y_1} = y_1^d - y_1 = V_x^d - V_x$ and $e_{y_2} = y_2^d - y_2$. The choice of the parameters α_1, α_2, $K_P^{y_1}$, $K_I^{y_1}$, $K_P^{y_2}$ and $K_I^{y_2}$ is straightforward. Equations (22) and (23) yield respectively the estimation of F_1 and F_2.

3.4 Model-free vehicle control and natural outputs

In order to be totally parameter-independent, consider the following natural outputs, which can be obtained through direct measurements:

$$\begin{cases} y_1 = \text{longitudinal speed} \\ y_2 = \text{lateral deviation} \end{cases}$$

The first output remains the measured (or well estimated) longitudinal velocity, and the second one is now given by the lateral deviation which is also supposed to be accessible from on line measurements. The two control variables are the same as in Section 3.3. Newton's second law then yields the two ultra-local models:

$$\text{longitudinal motion: } \dot{y}_1 = F_1 + \alpha_1 u_1 \qquad (24)$$

$$\text{lateral motion: } \ddot{y}_2 = F_2 + \alpha_2 u_2 \qquad (25)$$

Note the following properties:

- Equations (24)-(25) are "decoupled,"
- Equation (25) is of order 2 with respect to the derivative of y_2. This is the second example of such a property (see Section 3.2.1).

Considering the motion in Equation (24) (resp. (25)), the loop is closed by an iP (21) (resp. iPD (18)).

4. SIMULATION RESULTS

The simulations are carried out under MATLAB using a nonlinear 10Dof model of an instrumented Peugeot 406 car as in Menhour *et al.* [2013]. The reference signals shown by grey curves in Figures 4, 5 and 6 are experimental recorded data. Figures 4, 5 and 6 demonstrate that our new model-
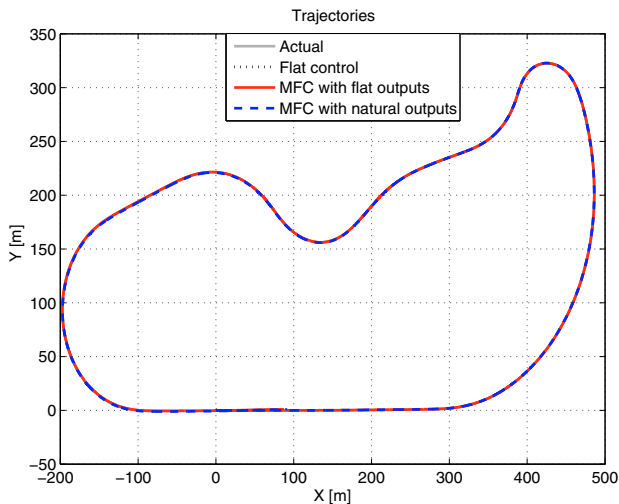

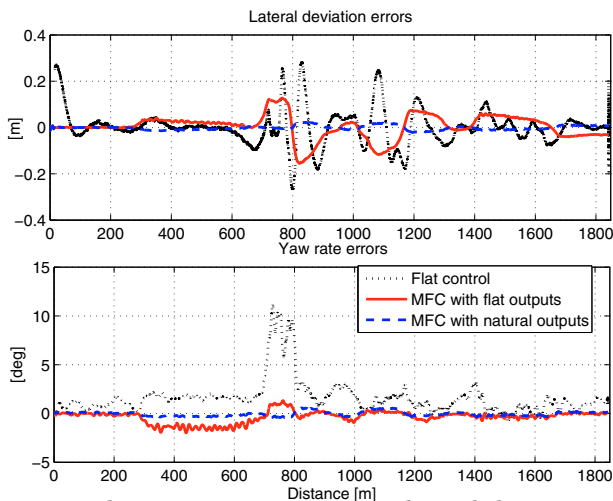Fig. 4. Desired trajectory versus the trajectories of controlled models

Fig. 5. Tacking trajectory errors on lateral deviation and yaw angle

free setting with natural outputs gives quite satisfactory results. They are much better than those resulting from model-free control associated to the flat outputs. It should be pointed out that the test track which has been considered implies strong lateral and longitudinal dynamical loads. This track involves different types of curvatures linked to straight parts, and all these configurations represent a large set of driving situations. Figure 4 shows that model-free control with natural outputs yields accurate enough behavior for autonomous driving applications. According to the results displayed on Figure 5, the lateral error is less than $2\,cm$. Concerning the yaw angle output, the resulting error is limited to $0.51\,deg$. Note that the lateral errors associated to the flatness-based control and the model-free control with the flat outputs are higher than $10\,cm$. The resulting yaw angle errors are higher than
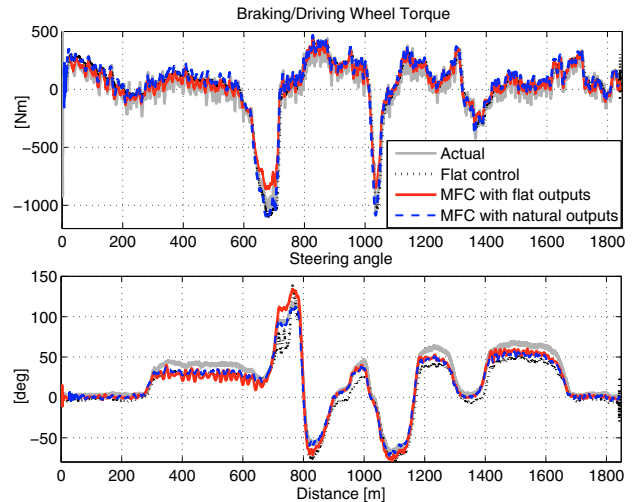

Fig. 6. Wheel torques and steering angles control signals: actual and those obtained with new model-free control and the one proposed in Menhour *et al.* [2013]

$10\,deg$ for flatness-based control, and $1\,deg$ for model-free control with flat outputs. Figure 6 shows that the control signals computed from the model-free control with natural outputs are closed to the actual ones provided by the driver along the track.

5. CONCLUSION

The path followed by the authors for the control of autonomous wheeled cars leads to a design which is both easy to implement and to grasp. The viewpoint, which we now advocate, has been successfully tested under "normal" driving conditions through an advanced simulation platform environment (see Menhour *et al.* [2015] for more details). However, in order to be fully convincing, other tests have to be handled on a real embedded vehicle under severe driving conditions. This will be reported in forthcoming publications.

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